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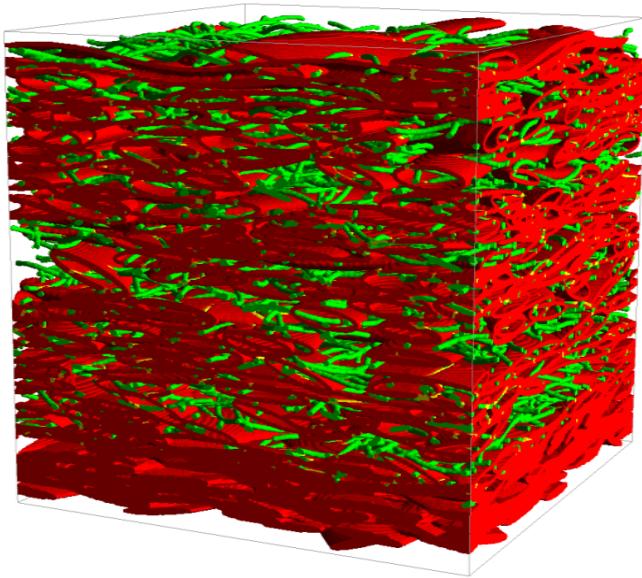
# Determination of the capillary pressure – saturation relation for paper based on its 3D microstructure

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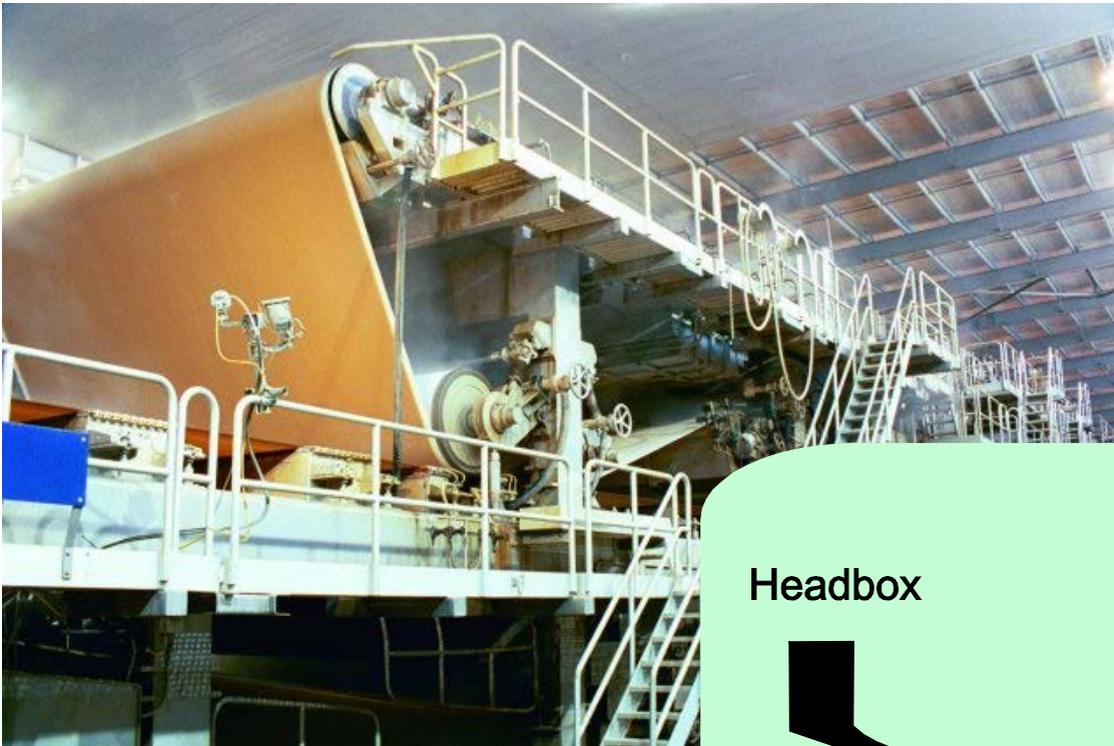
# Overview

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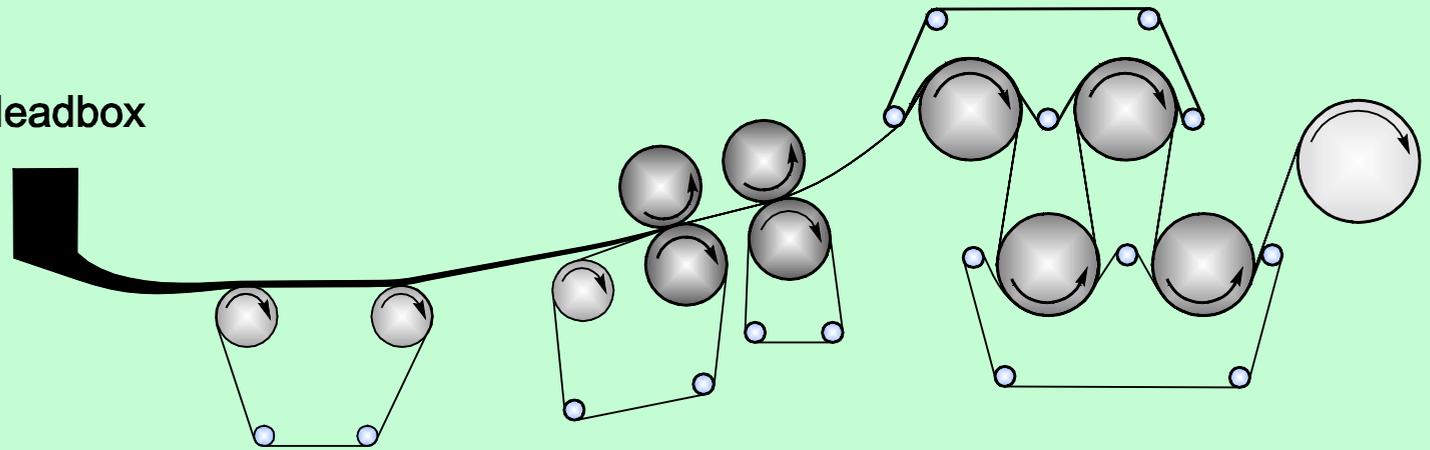
- Motivation: Paper Research at Fraunhofer ITWM
- Virtual Paper Generation
- New Multiple Contact Angle Pore Morphology Method
- Capillary Pressure – Saturation Curves of Virtual Paper
- Application and Summary

# Paper Research at Fraunhofer ITWM

Paper Machine



Headbox



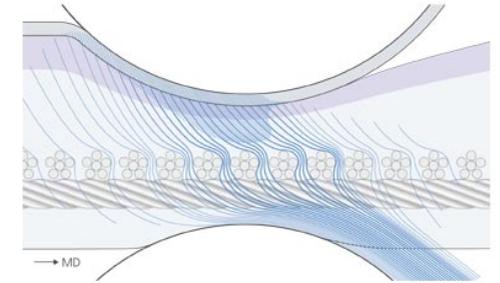
Forming Section

Pressing Section

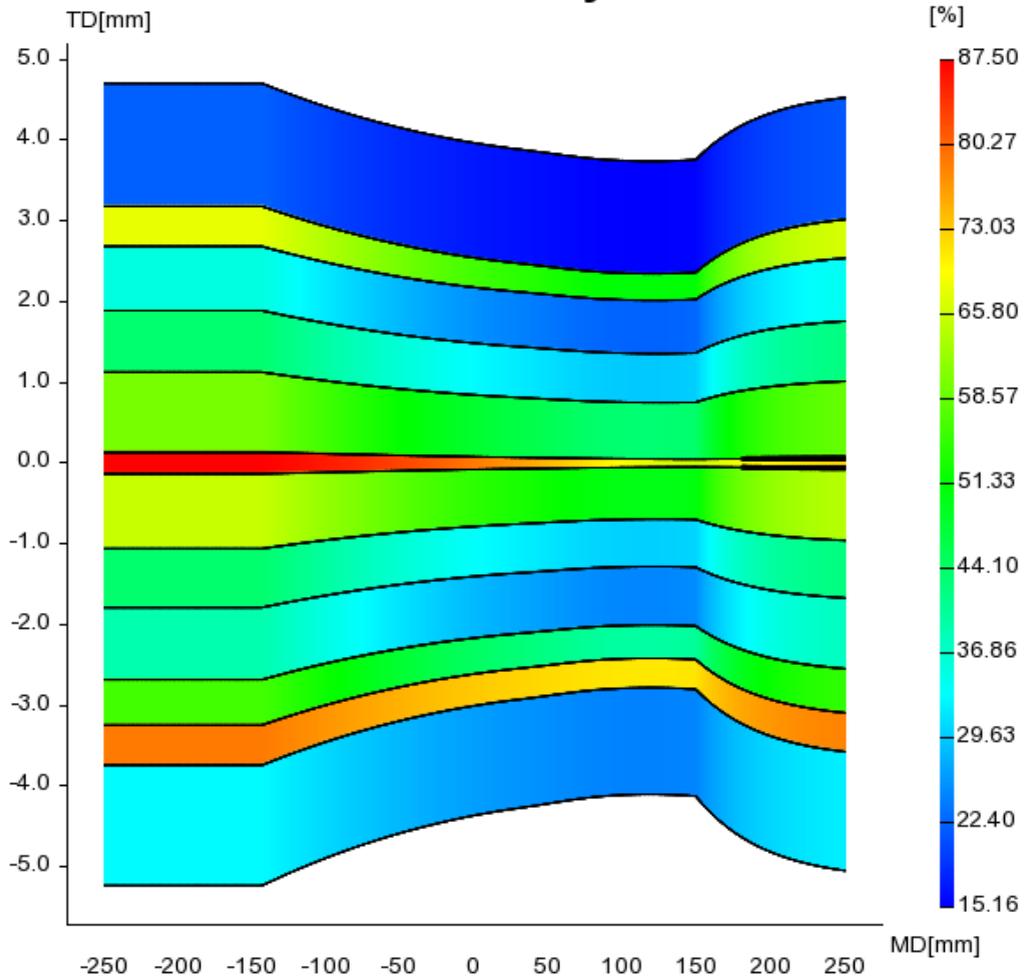
Drying Section

# Paper Research at Fraunhofer ITWM

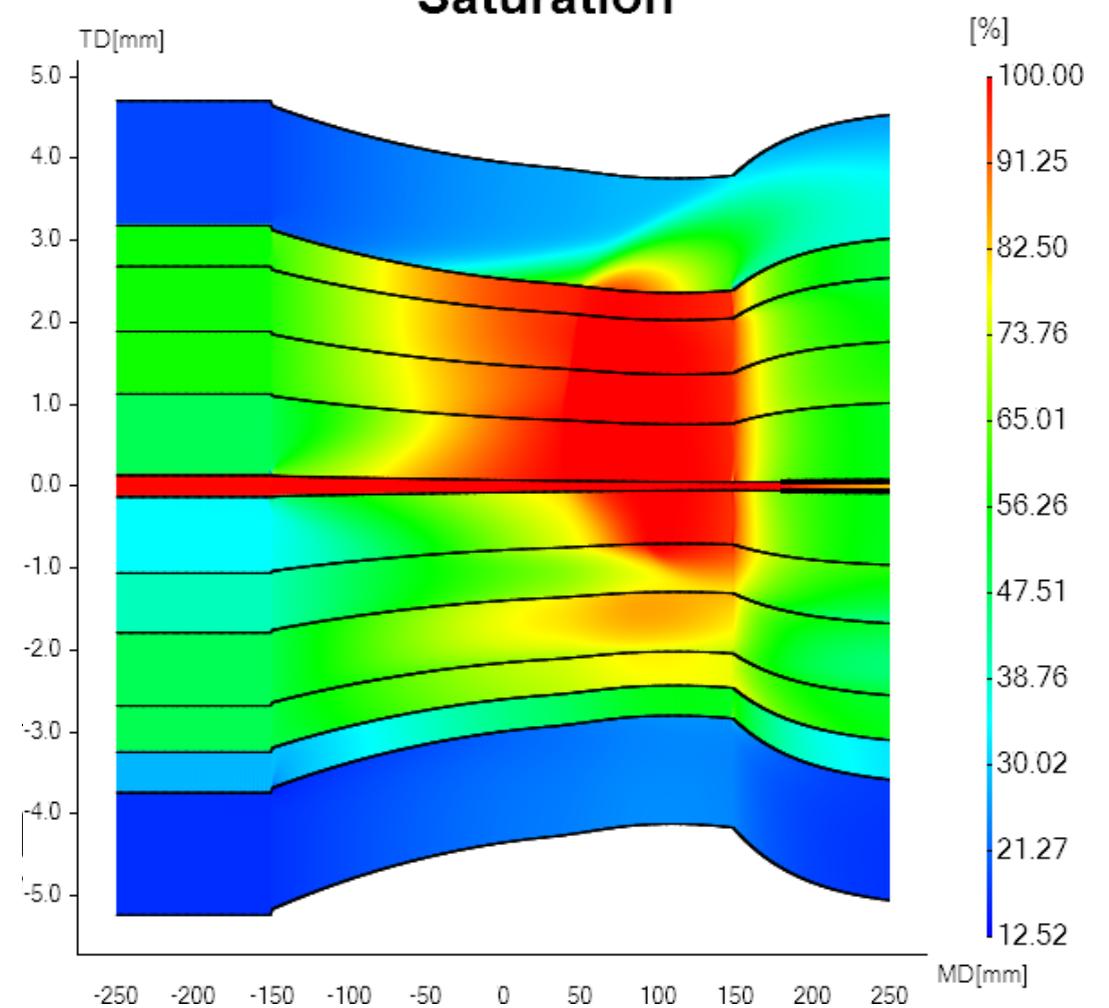
## Macro simulation of the press nip



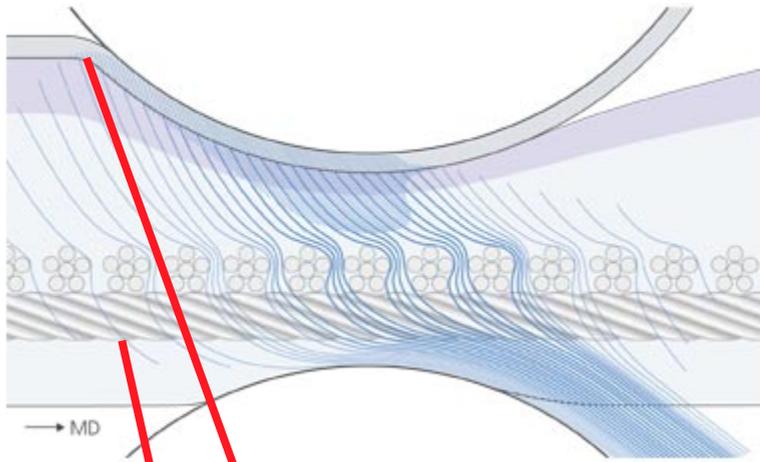
### Porosity



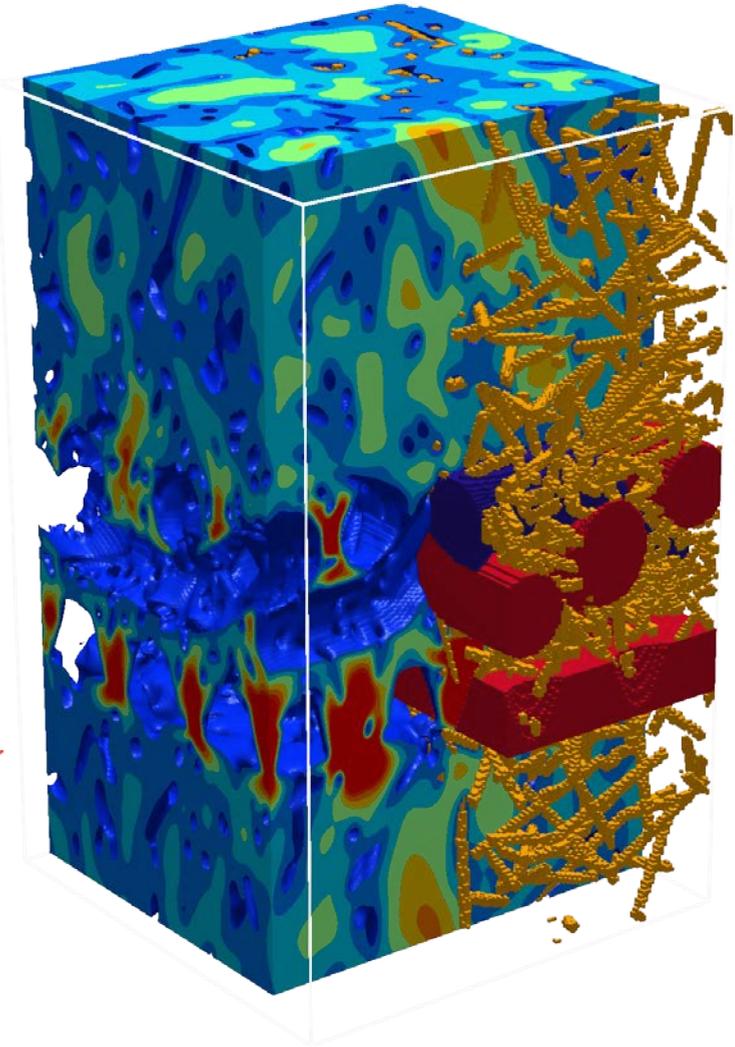
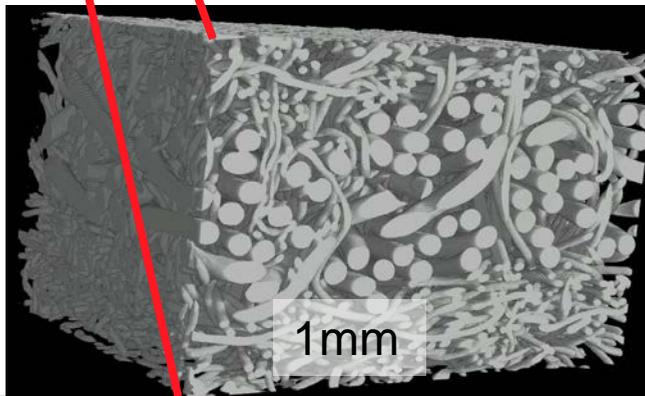
### Saturation



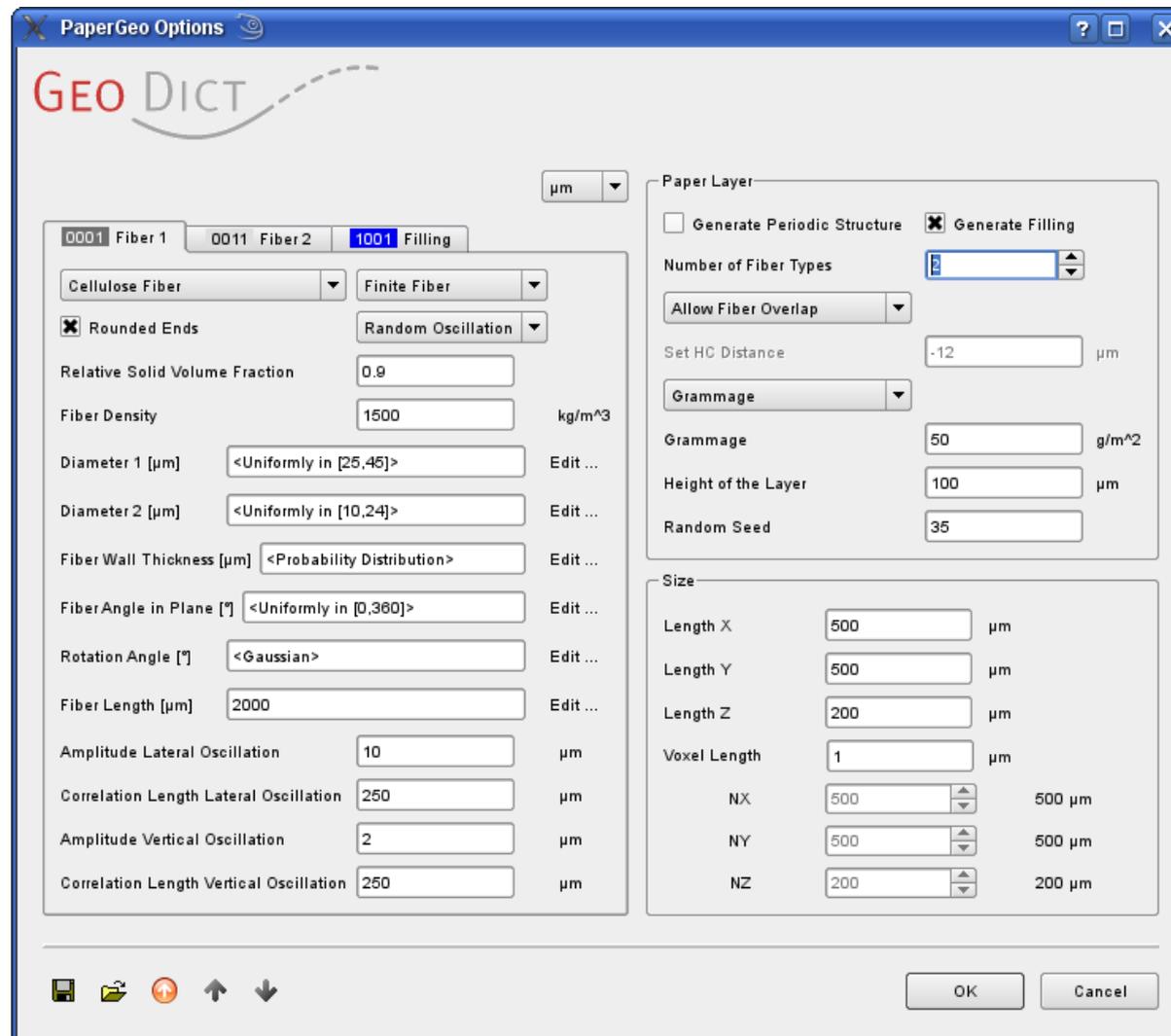
# Paper Research at Fraunhofer ITWM



Press Nip



# Virtual Paper Generation



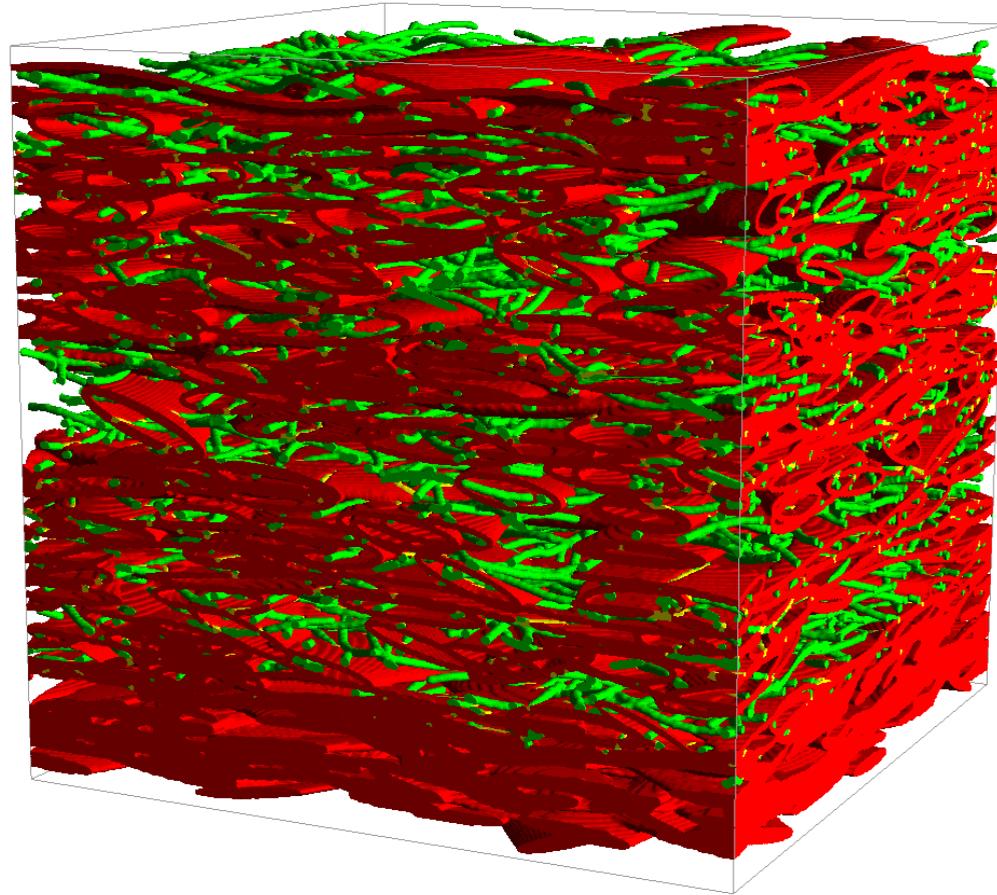
Use **PaperGeo** to generate realistic paper models

## Parameters

- Cellulose, ellipsoidal, and circular fibers
- Fillers and fines
- Random structure
- Fiber lay down

# Virtual Paper Generation

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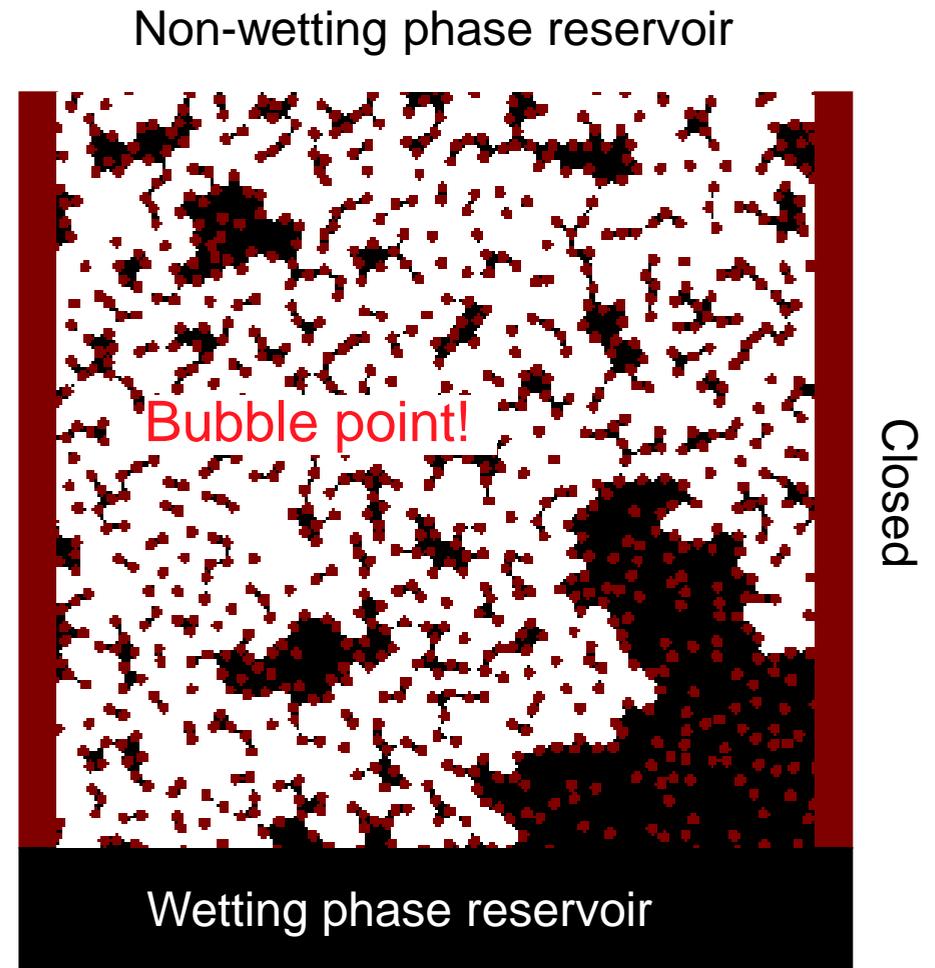


# Simulation of wetting and non-wetting phase distribution

- Solving two-phase Navier-Stokes equation requires large resources
- We use a morphological operations are used to simulate the phase distribution according to a drainage experiment (Hilpert et al. 2001)
- Drainage of the wetting phase if

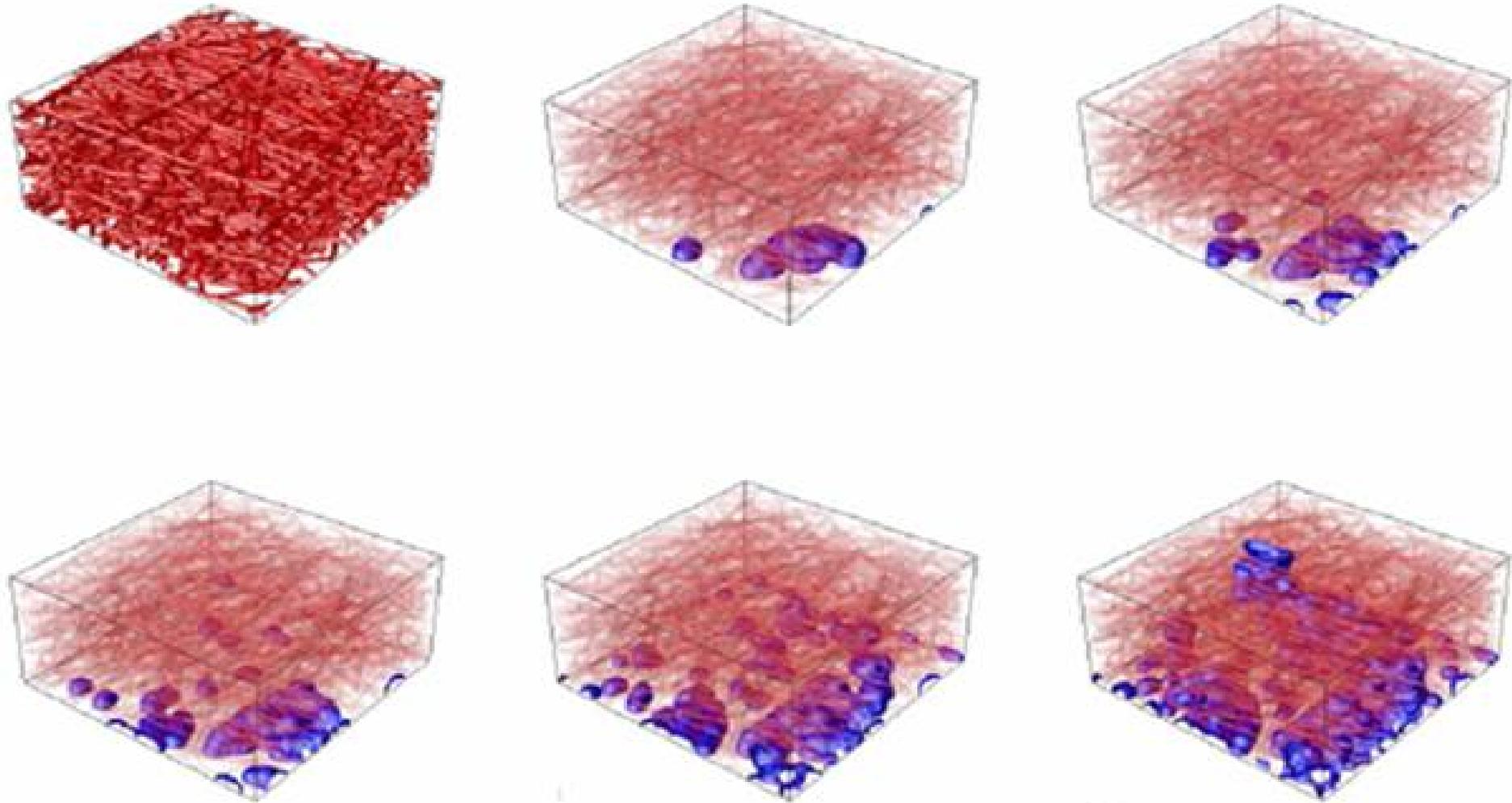
$$p_c \geq \frac{2\sigma}{r} \cos \theta$$

- Initial conditions:  
Void space is completely filled with wetting phase
- Algorithm based on the calculation of the Euclidean distance



# Illustration of the wetting phase distribution

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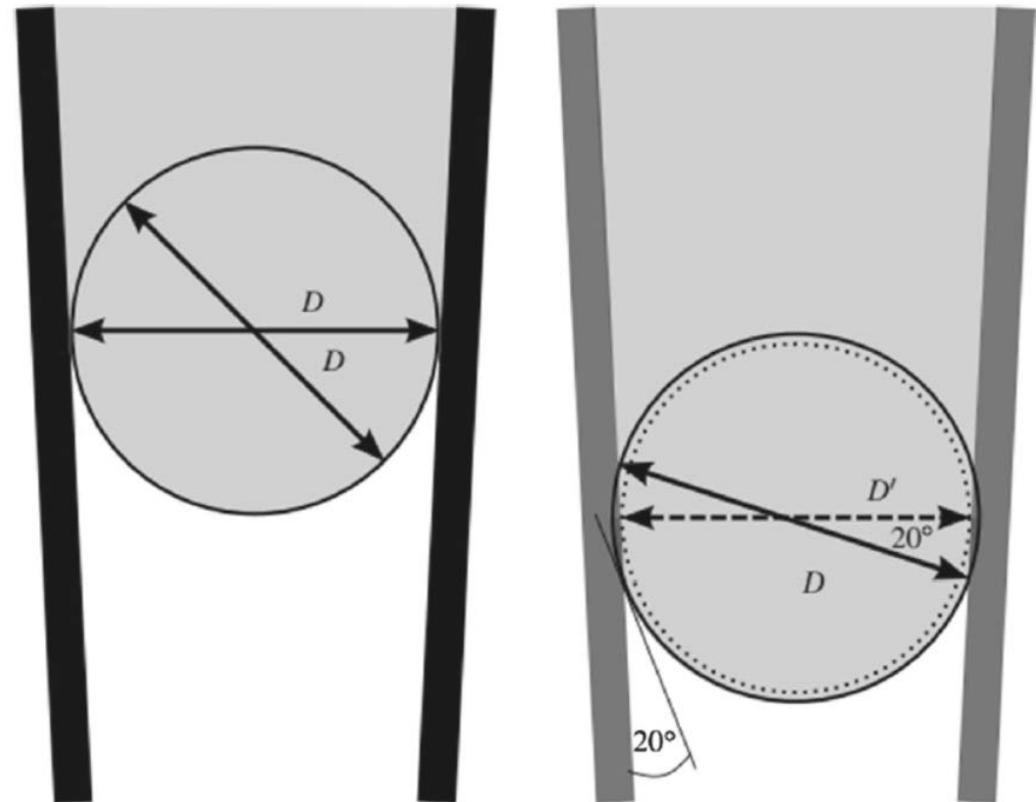
# New Multiple Contact Angle Pore Morphology Method

- For totally wetting (left hand side), the meniscus is determined by a sphere of diameter  $D$

$$p_c = \frac{4\sigma}{D}$$

- For partially wetting (right hand side), the meniscus is determined by a sphere of diameter  $D'$ , where

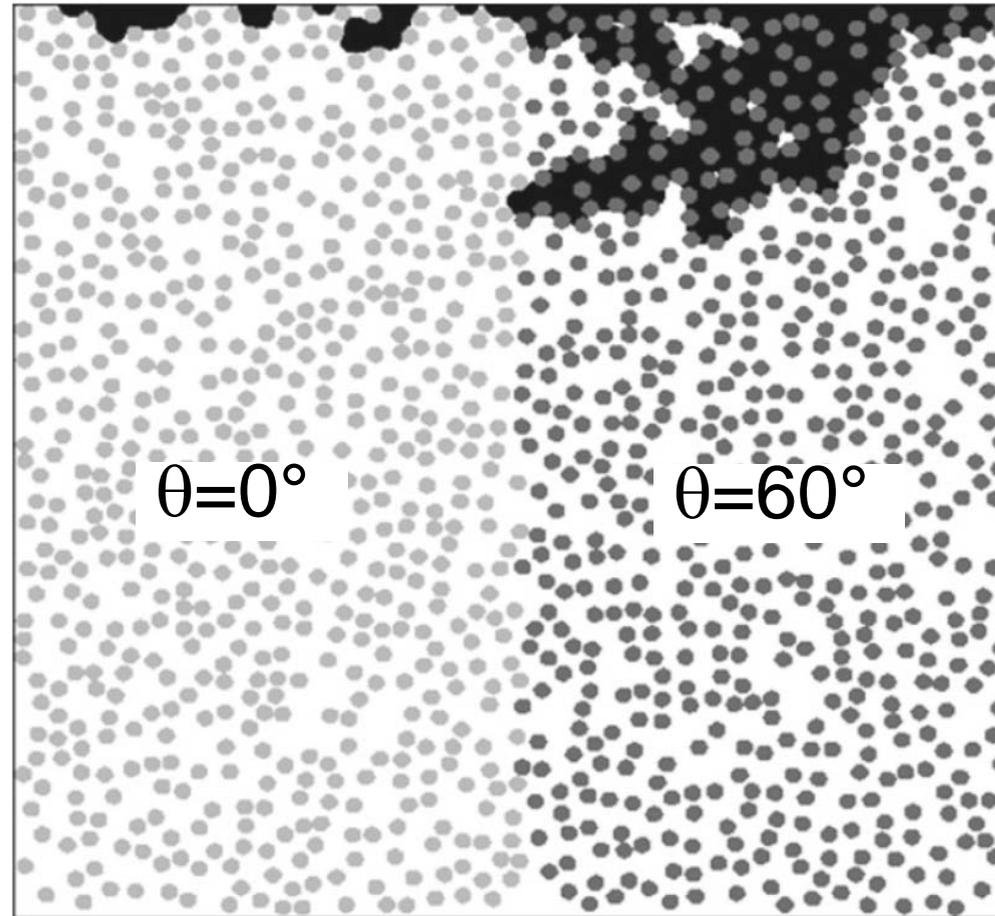
$$p_c = \frac{4\sigma}{D} \cos \theta \quad D' = D \cdot |\cos \theta|$$



Volker P. Schulz, Eric A. Wargo and Emin C. Kumbur: „Pore-Morphology-Based Simulation of Drainage in Porous Media Featuring a Locally Variable Contact Angle“, Transp Porous Med (2015) 107:13–25

# Porous media with locally different contact angle

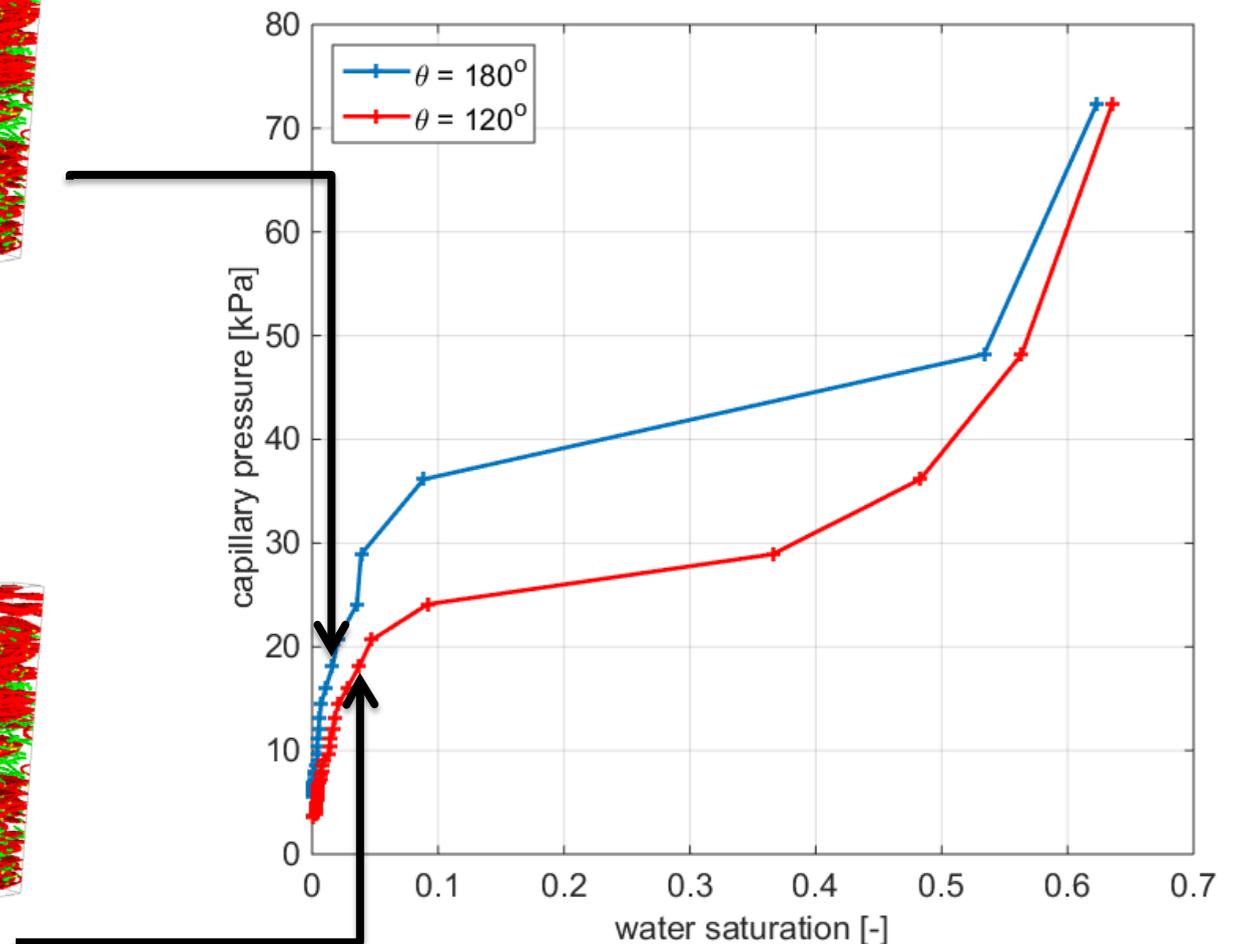
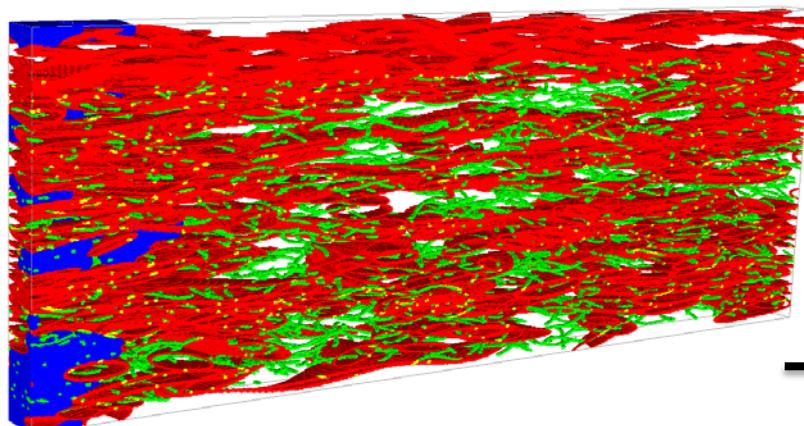
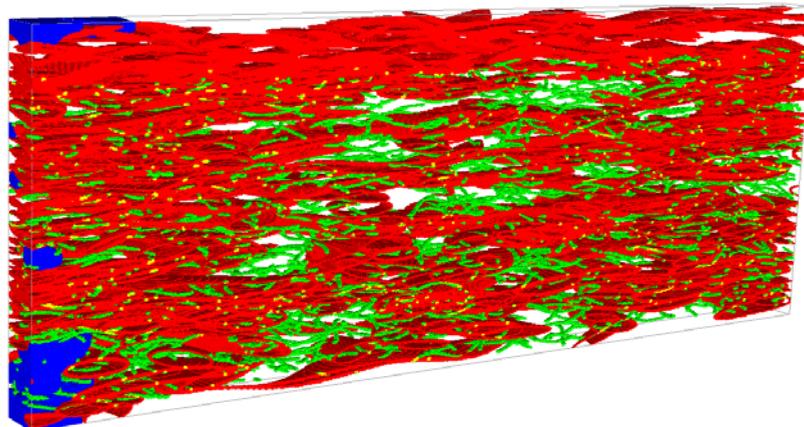
Locally variable contact angle leads to (locally) different saturation at the same capillary pressure



# Application to 3D microstructures of paper

Two different fibers, 50x384x1000 voxel, resolution of 1  $\mu\text{m}/\text{voxel}$

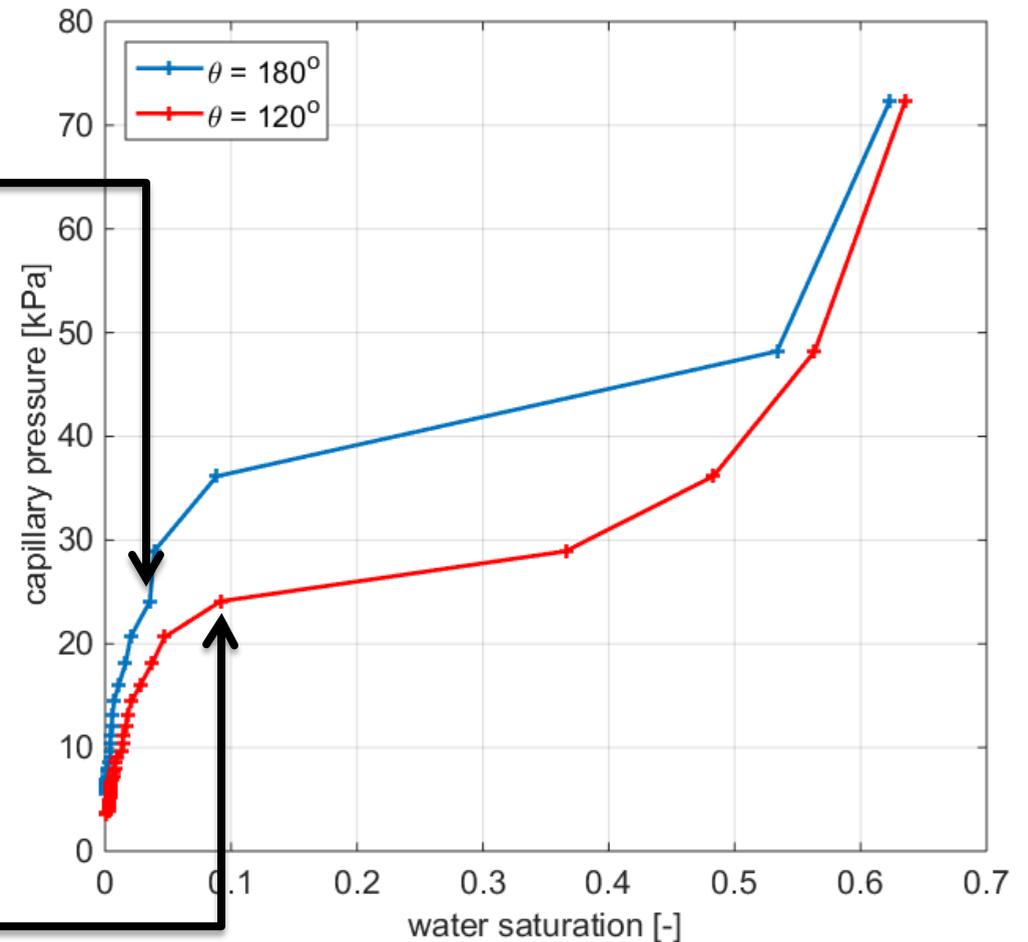
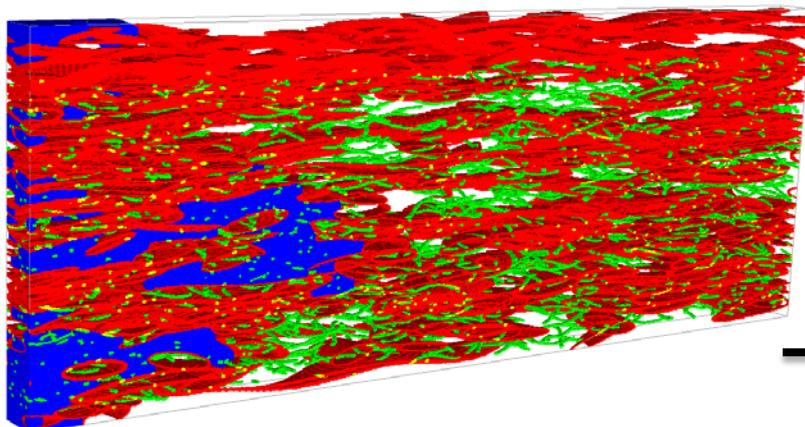
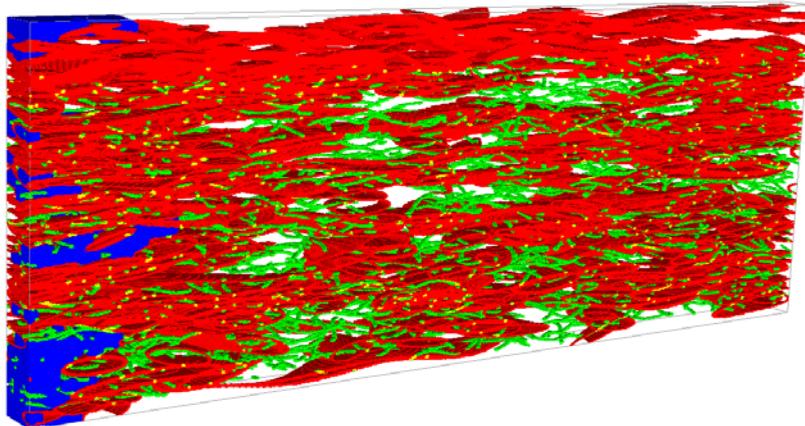
Contact angles are: 155° (red) and 120° (green, top), 180° (green, bottom)



# Application to 3D microstructures of paper

Two different fibers, 50x384x1000 voxel, resolution of 1  $\mu\text{m}/\text{voxel}$

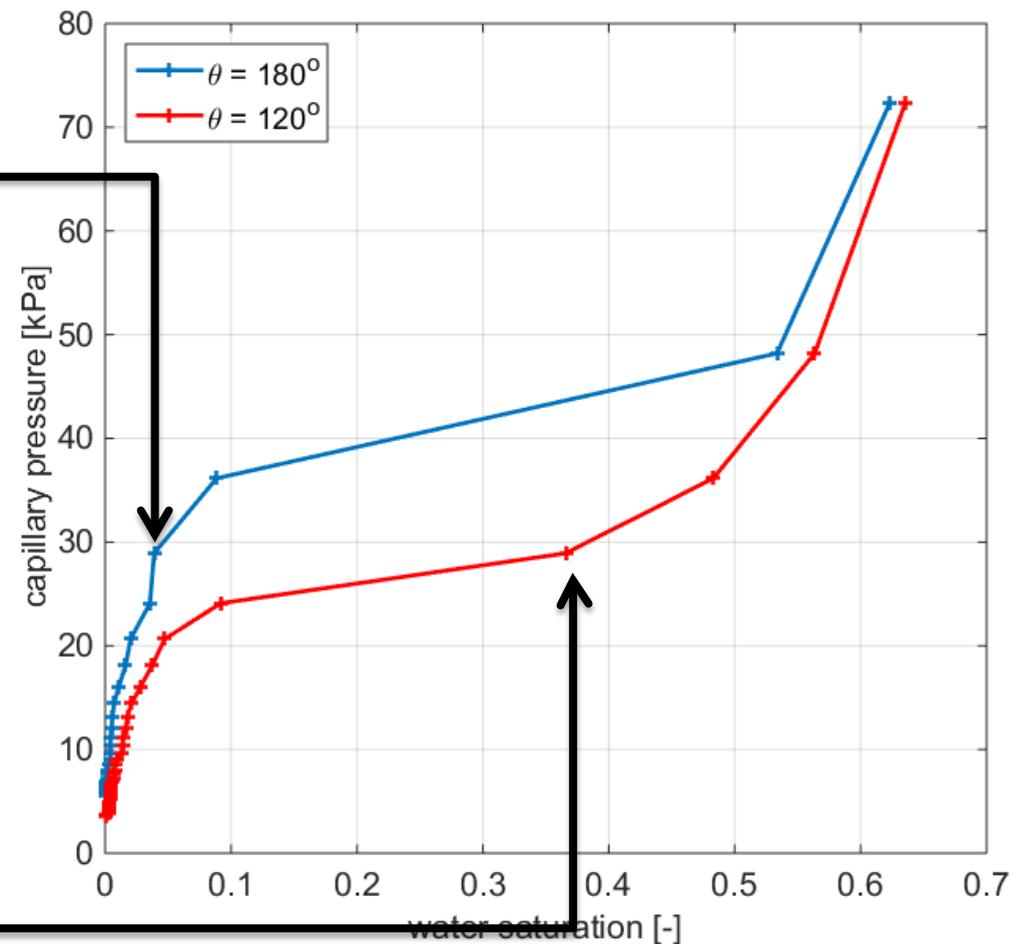
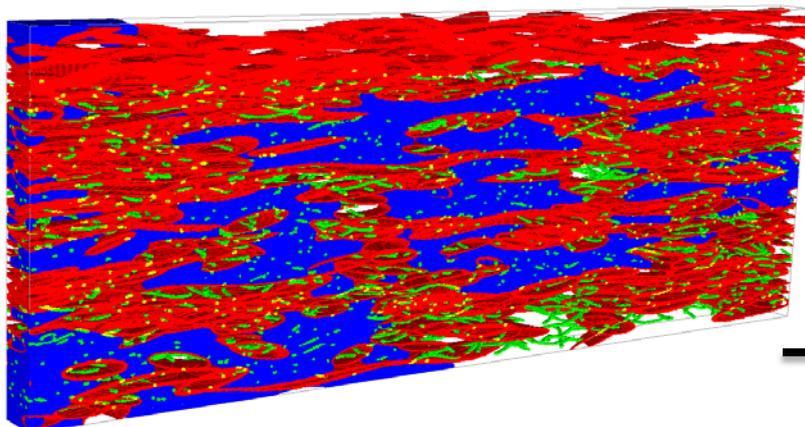
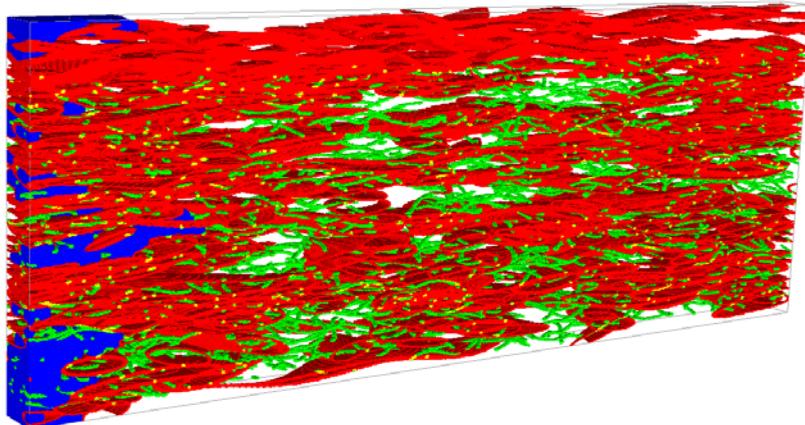
Contact angles are: 155° (red) and 120° (green, top), 180° (green, bottom)



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Two different fibers, 50x384x1000 voxel, resolution of 1  $\mu\text{m}/\text{voxel}$

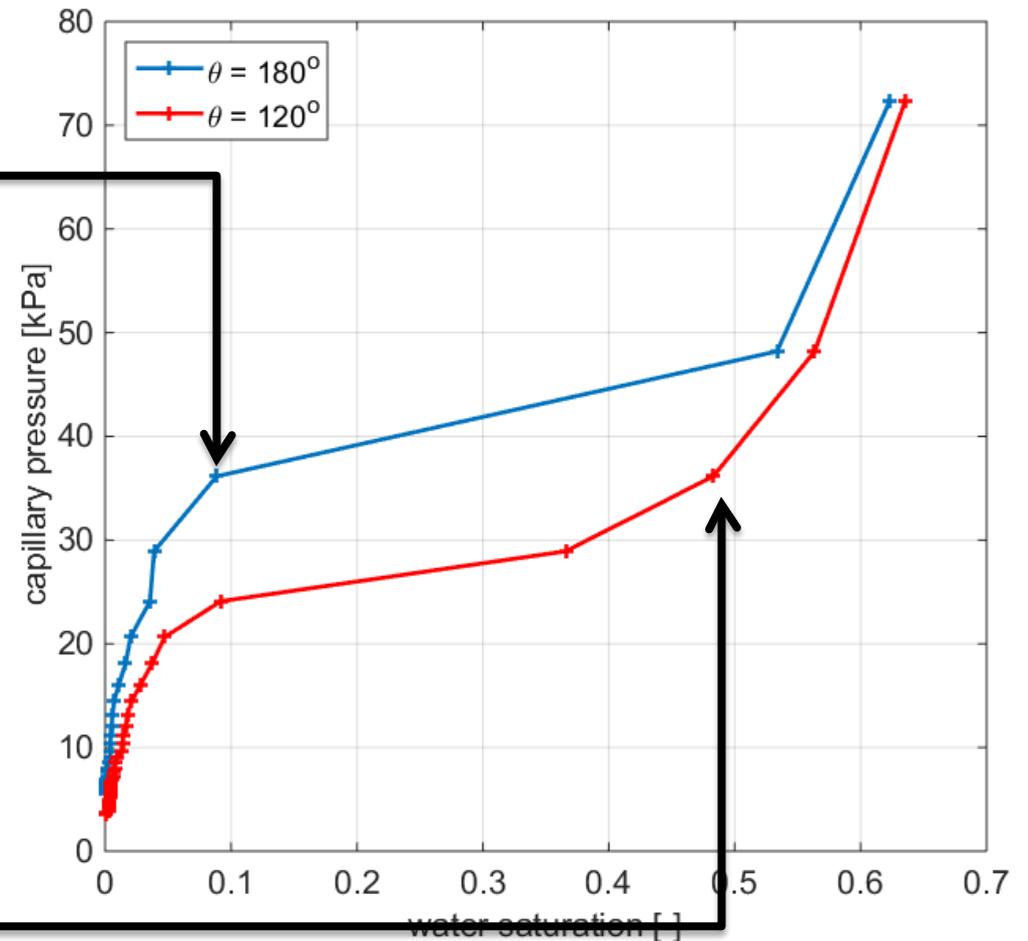
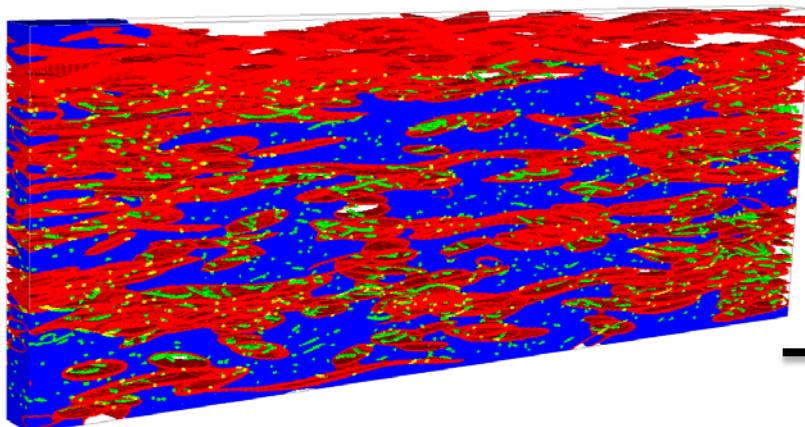
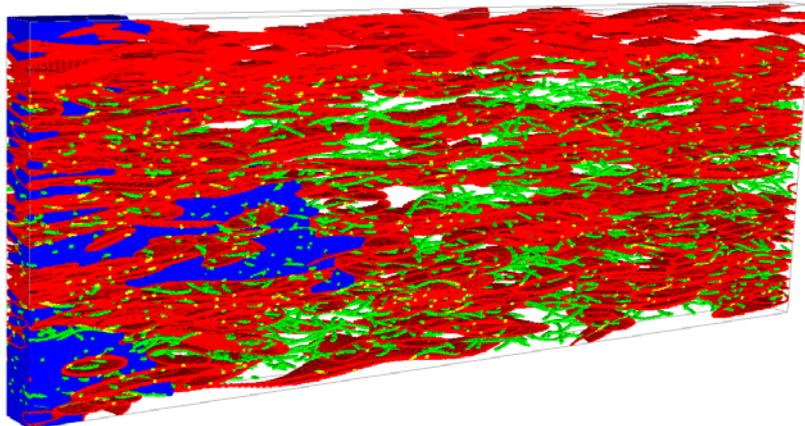
Contact angles are: 155° (red) and 120° (green, top), 180° (green, bottom)



# Application to 3D microstructures of paper

Two different fibers, 50x384x1000 voxel, resolution of 1  $\mu\text{m}/\text{voxel}$

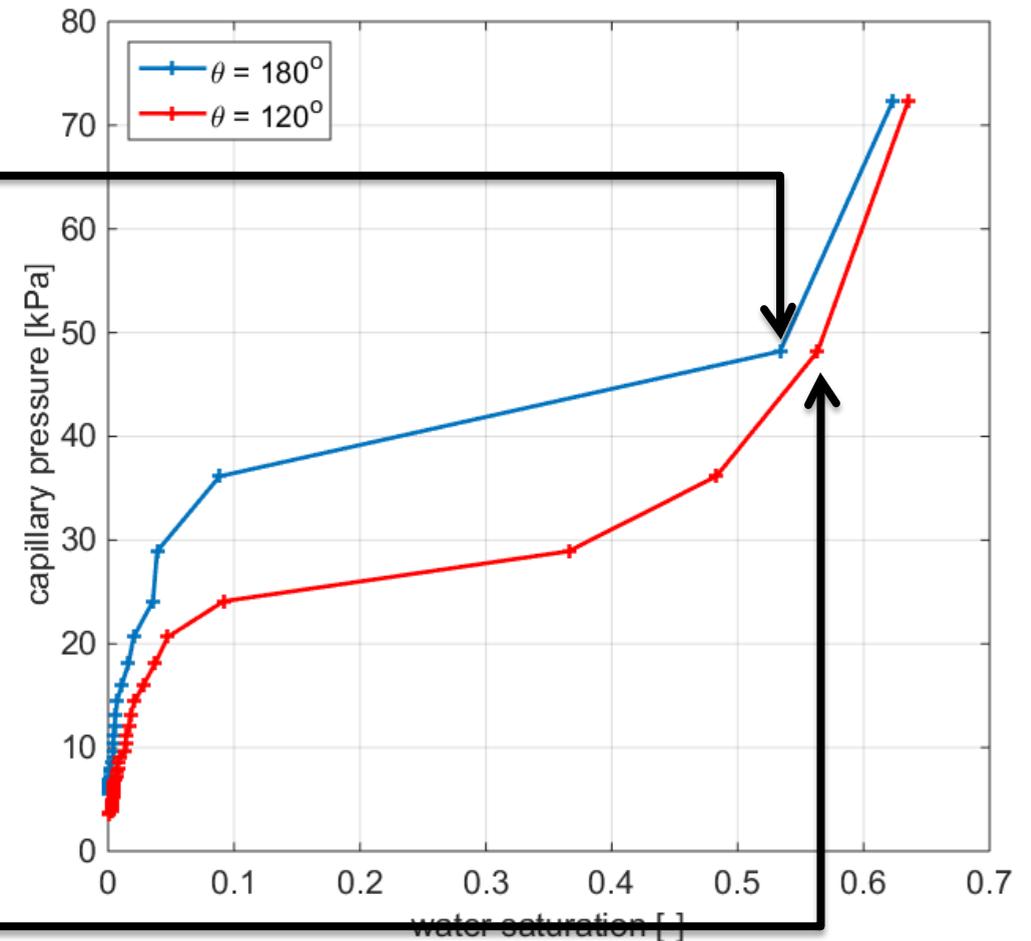
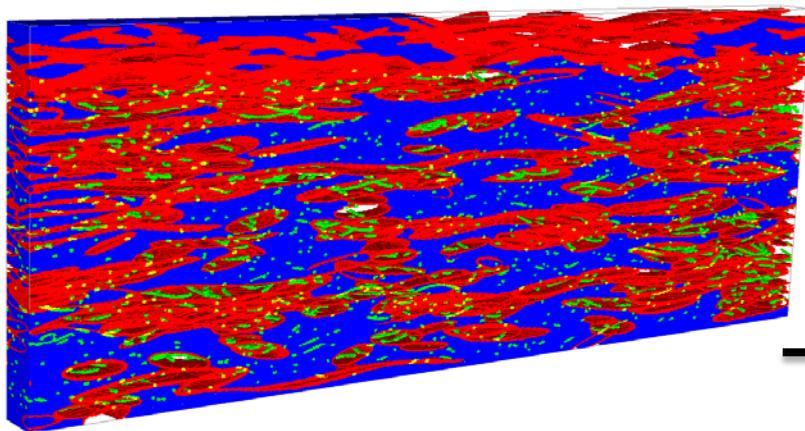
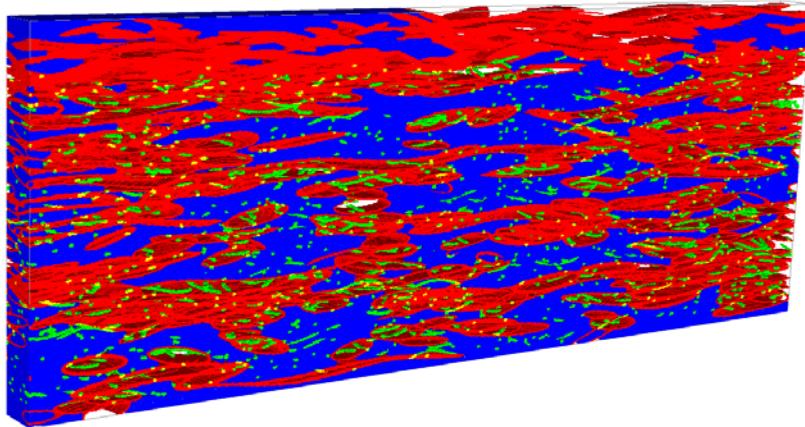
Contact angles are: 155° (red) and 120° (green, top), 180° (green, bottom)



# Application to 3D microstructures of paper

Two different fibers, 50x384x1000 voxel, resolution of 1  $\mu\text{m}/\text{voxel}$

Contact angles are: 155° (red) and 120° (green, top), 180° (green, bottom)



## Application to paper and summary

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- The pore morphology simulation has been already successfully used to simulate the paperboard edge wicking

A. Mark, J. Tryding, J. Amini, F. Edelvik, M. Fredlund, E. Glatt, R. Lai, L. Martinsson, U. Nyman, M. Rentzhog, S. Rief and A. Wiegmann: „Modeling and simulation of paperboard edge wicking”, Nordic Pulp and Paper Research Journal, Vol 27, No.2/2012, pp. 397-402

- In this approach, the capillary pressure-saturation relation is used in a multi scale model

- With the shown extension, one can study 3D micro structures of paper featuring locally variable contact angles
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